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COMPLEX FORMATION IN A QUATERNARY RECIPROCAL SYSTEM OF
CHLORIDES, SULFATES, AND TUNGSTATES OF LITHIUM AND POTASSIUM

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As it is known, in the case when the components of a quaternary reciprocal system crystallize out in pure state and do not form solid solutions, the volume of the prism resolves into six volumes of crystallization of the six components (anions) of the system. The prism $\text{Li, K} // \text{Cl, SO}_4$ studied by H. P. Landolt¹ may be cited as an example. In this case the prism can be divided by two stable ternary sections into three stable tetrahedrons in each of which there is a quaternary eutectic. In case of appearance in the system of a series of solid solutions, the number of crystallization volumes is decreased, as is the number of stable tetrahedrons. For example in the ternary reciprocal system $\text{Li, K} // \text{Cl, SO}_4$, studied by H. S. Ruzhkovskaya², the number of crystallization volumes from the prism is reduced to three and the prism is cut (divided) into two stable tetrahedrons.

In case of complex formation between the individual components, the phase diagram of such a system as well as its analysis are further complicated. The number of stable crystallization volumes and the stable tetrahedral sections is decreased. An illustrative example of such a system is the one studied by the authors in the help of the visual polythematic method³ - namely the quaternary reciprocal system $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$.

The above system, if depicted, as usual, as a three sided right-angled prism, is complicated by the presence of two double salts, the $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ and $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{WO}_4$ on the opposite sides of the prism. This diagram was first drawn by the authors during the study of the ternary reciprocal system $\text{Li, K} // \text{SO}_4, \text{WO}_4$.

The tetrahedron describing the above reciprocal system, shown in Figure 1, is obtained by depicting the presence of congruently melting complex compositions, $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ on the Li_2SO_4 - K_2SO_4 binary side, with a maximum at 625°C and $25\text{ mol } \text{Li}_2\text{SO}_4$ on the Li_2SO_4 - K_2WO_4 binary side with a maximum at 735°C .

Reduction of the space diagram
for the reciprocal salt pair
system $\text{Li, K} // \text{SO}_4, \text{WO}_4$
on the composition square

Fig. 1



* Of the double salt type

** The $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ and the $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{WO}_4$ double salts are shown as Li_2SO_4 and Li_2WO_4 respectively in this article.

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The melting point data pertaining to the $\text{Li, K} // \text{SO}_4, \text{WO}_4$ system are listed in Table 1.

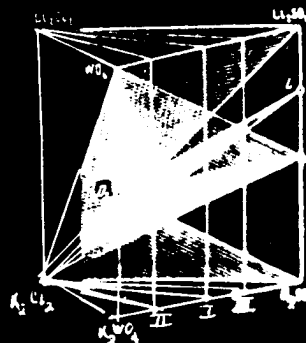
Binary $\text{Li}_2\text{WO}_4\text{-K}_2\text{WO}_4$		Binary $\text{Li}_2\text{SO}_4\text{-K}_2\text{SO}_4$	
% K_2WO_4	$t, ^\circ\text{C}$	% K_2SO_4	$t, ^\circ\text{C}$
0		0	804
5		5	808
10		10	813
15		15	818
20		20	823
25		25	828
30		30	833
35		35	838
40		40	843
45		45	848
		50	853
		55	858
		60	863
		65	868
		70	873
		75	878
		80	883
		85	888
		90	893
		95	898
		100	903

The surf... liquidus system consist... Fields of crystallization, two of which are the crystallization fields of $\text{Li}_2\text{WO}_4\text{-K}_2\text{WO}_4$ and $\text{Li}_2\text{SO}_4\text{-K}_2\text{SO}_4$, occupying correspondingly the 10.04 and 21.8% areas, while the other four fields pertain to the pure components.

The fields of potassium sulfate, lithium sulfate and lithium tungstate are further broken up into the and modification areas. Situated on opposite sides of the composition square the two double salts (complexes) establish the principal characteristics of the system and displace the equilibrium to the side of the newly formed stable section $\text{Li}_2\text{WO}_4\text{-K}_2\text{WO}_4\text{-Li}_2\text{SO}_4\text{-K}_2\text{SO}_4$, which bisects the composition square into two quadrangles which triangulate in turn to two phase triangles. (See Fig. 2). In the system the complex forming reaction on the two opposite sides of the composition square is predominant to the double decomposition reaction. The system $\text{Li, K} // \text{SO}_4, \text{WO}_4$ is classified as reciprocal system of the salt-a-diagonal type. In order to verify the stability of the two complexes (double salts) $\text{Li}_2\text{WO}_4\text{-K}_2\text{WO}_4$ and $\text{Li}_2\text{SO}_4\text{-K}_2\text{SO}_4$ in the quaternary reciprocal system $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$ the "inside" of prism composition was studied by means of determination of its various sections, in particular the three "book" sections (I, II, III,) and the five triangular sections, as shown in Fig. 2.

Scheme of Sections through a prism of composition for the system $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$

Fig. 2



* The "book" sections the authors conditionally define as systems and thus treat them as such in their investigations.

reciprocal

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In the article the authors describe only the sections of the system that pertain directly to the above mentioned double salts D_1 and D_2 and which define the boundaries of their crystallization volumes.

It is first necessary to define and elaborate on the three "book" sections:

I "Book" Section -



II "Book" Section -



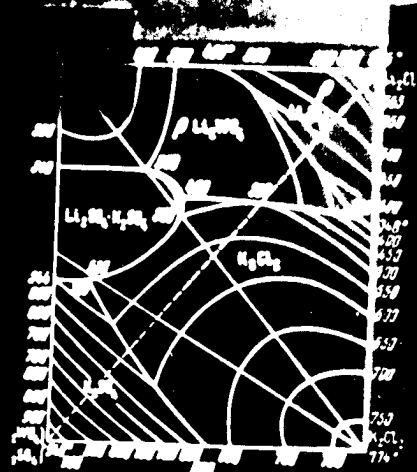
III "Book" Section -



The "book" representing the I "Book Section", as shown in Fig. 3, is a ternary diagram (Fig. 3) of the binary system Li_2SO_4 - K_2SO_4 with a vertical axis of Li_2SO_4 and three sections, of which one is made through the point $(50\% \text{Li}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4) - (50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4)$ and to determine the solubility of a congruently melting double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$. The sections are made through ternary systems describing the solubility of the double salt in the $(50\% \text{Li}_2\text{SO}_4 + 50\% \text{Li}_2\text{SO}_4) - \text{Li}_2\text{SO}_4$ and $(50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4) - \text{K}_2\text{SO}_4$ and the $(50\% \text{Li}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4) - \text{Li}_2\text{SO}_4$ and $(50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4) - \text{K}_2\text{SO}_4$. The I "Book Section" is subdivided into three sections: the first is that of the double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$, the second is that of the pure component salts.

Scheme of I "Book Section"

Fig. 3



*In using the prism to describe the quaternary reciprocal system, the reciprocal systems therein would naturally be represented as rectangles.

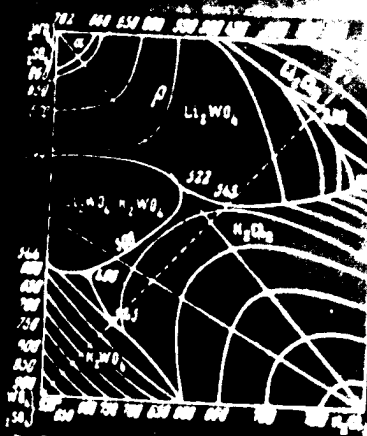
The field of crystallization of the double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ is flat in appearance, characterized by almost completely horizontal isotherms, as this double salt melts without decomposition and the isotherms of stability and displaces the crystallization fields of pure components. Potassium chloride exhibits isotherms that curve upward. The potassium tungstate field shows a steep slope, as seen from the closely situated isotherms. The lithium tungstate field exhibits the λ and β homeomorphic forms. The lithium tungstate field is characterized by its elongated form and the upwardly curving isotherms. In this section the complex forming reaction is predominant.

Thus the I "Book Section" establishes that the double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ is congruently melting, stable and is found to occupy 10.68% of the total surface of the "Book Section." It is further characterized by the flatness of the double salt field with an almost complete absence of isotherms.

- The rectangle representing the II "Book Section", shown in Fig. 4, is characterized by:
- 1) A binary system $\text{Li}_2\text{Cl}_2 - \text{K}_2\text{Cl}_2$ with a eutectic at 346°C and 46.5% K_2Cl_2 .
 - 2) A section through a reciprocal system ($80\% \text{Li}_2\text{WO}_4 + 20\% \text{K}_2\text{WO}_4$ - $80\% \text{K}_2\text{WO}_4 + 20\% \text{Li}_2\text{WO}_4$) characterized by the presence of the double salt $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{WO}_4$.
 - 3) A section through the top of the prism ($80\% \text{Li}_2\text{WO}_4 + 20\% \text{Li}_2\text{SO}_4$) - $80\% \text{K}_2\text{WO}_4 + 20\% \text{K}_2\text{SO}_4$ with a univariant point at 475°C and 46.5% ($80\% \text{Li}_2\text{WO}_4 + 20\% \text{Li}_2\text{SO}_4$).
 - 4) A section through the bottom of the prism ($80\% \text{K}_2\text{WO}_4 + 20\% \text{K}_2\text{SO}_4$) - $80\% \text{Li}_2\text{WO}_4 + 20\% \text{Li}_2\text{SO}_4$ with a univariant point at 600°C and 45% K_2Cl_2 .

Scheme of II "Book Section"

Fig. 4



The surface of the rectangular II "Book Section" shows five distinct fields (volumes) of crystallization of which four are the fields of pure components while the fifth depicts the field of a double salt $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{WO}_4$. The field of crystallization of the double salt has a flat appearance, characterized by the absence of isotherms. It being congruently melting, the stability is preserved and even spread quite deeply into the inside volumes of the whole system. The field of lithium tungstate has an elongated appearance with isotherms showing upward and presence of the λ and β crystalline areas. The field of potassium chloride also shows isotherms curved upward, the curvature somewhat diminishing with decrease in temperature.

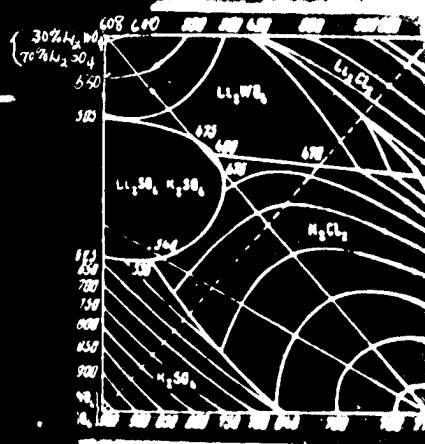
The field of potassium tungstate is distinguished by the steepness of isotherms, as shown by the closely spaced isotherms. In this section the congruent melting reaction is predominant. Thus the results of the analysis of II "Book Section" establishes the presence inside the section of a double salt field $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ occupying 9.9% of the total rectangular section. The field of this double salt has a flat appearance and is characterized by the absence of isotherms. Distinct from the field of the complex D_1 , the presence of the following fields is shown: Li_2Cl_2 (Δ and δ), K_2Cl_2 , K_2SO_4 and Li_2SO_4 (Δ and δ).

The rectangle representing the III "Book Section", as shown in Fig. 5, is composed by the following sections:

- 1) $(50\% \text{Li}_2\text{SO}_4 + 50\% \text{Li}_2\text{SO}_4) - (50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4)$, characterized by the presence of a congruent double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$.
- 2) $(50\% \text{Li}_2\text{SO}_4 + 50\% \text{Li}_2\text{SO}_4) - \text{Li}_2\text{Cl}_2$ with a monovariant point at 450°C and 50% ($50\% \text{Li}_2\text{SO}_4 + 50\% \text{Li}_2\text{SO}_4$).
- 3) $(50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4) - \text{K}_2\text{Cl}_2$ with a monovariant point at 450°C and 50% ($50\% \text{K}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4$).
- 4) A binary system $\text{Li}_2\text{Cl}_2 - \text{K}_2\text{Cl}_2$ with an eutectic at 340°C and 50% .

Scheme of III "Book Section"

Fig. 5



The crystallization surface of the system is composed of five fields: Li_2SO_4 , K_2SO_4 , Li_2Cl_2 , K_2Cl_2 , and $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$. Of these, only the field of the double salt, the others are those of pure components. The character of isotherms is the same as in the previously described sections (I and II). Again, as in the other two "Book Sections" the equilibrium system in the system is displaced toward complex formation.

Therefore, the III "Book Section" confirms that the double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$, being congruently melting, is stable and occupies a relatively large portion of the total volume of the prism of the overall system.

The data pertaining to the analyses of the two component sides of the three "Book" sections, on which the double salt compositions and characteristics are based, are listed in Table 2.

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Binary System		Binary System		Binary System	
Li ₂ WO ₄ -K ₂ SO ₄		Li ₂ SO ₄ -K ₂ SO ₄		Li ₂ SO ₄ -K ₂ SO ₄	
T, °C		T, °C		T, °C	
0	608	0	608	0	608
10	608	10	608	10	608
20	608	20	608	20	608
30	608	30	608	30	608
40	608	40	608	40	608
50	608	50	608	50	608
60	608	60	608	60	608
70	608	70	608	70	608
80	608	80	608	80	608
90	608	90	608	90	608
100	608	100	608	100	608

Analysis of the data allows the following observations and conclusions to be made: the three "book" sections confirm the presence of 8 different volumes of crystallization in the prism of Li, K // Cl, SO₄, WO₄ - two double salt volumes and six single component volumes, as shown in Fig. 6. The Li₂SO₄-K₂SO₄ double salt is also confirmed inside the prism by the study of "book" sections I and III. The double salt (complex) forming reaction in all three "book" sections is predominant over the equilibrium exchange reaction. In this manner, the Li₂SO₄-K₂SO₄ double salt, being congruently melting, maintains its stability even inside the prism. The Li₂SO₄-K₂SO₄ double salt crystallization volume is found to be a relatively large portion of the total prism volume and even somewhat displaces the crystallization volume of the other double salt, namely the Li₂WO₄-K₂WO₄, which is situated on the opposite side of the prism.

Inner crystallization volumes in a prism of composition for the system Li, K // Cl, SO₄, WO₄.

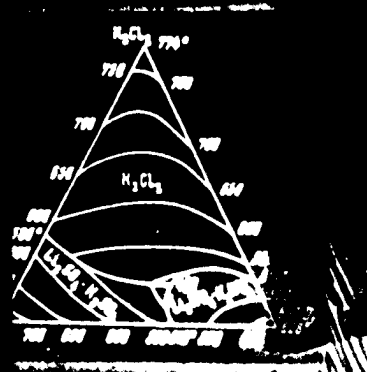
Fig. 6



The second double salt, $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{SO}_4$, is confirmed in the "back" section II. The double salt (complex) forming reaction in the "back" section II is also predominant but to a much lesser extent than in the other two "back" sections. This is confirmed by the smaller volume of the tungstate double salt $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{SO}_4$ as compared to the sulfate double salt $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$. Moreover the formation of the above mentioned double salts and their stability is further confirmed in one of the most interesting inner triangular sections: $(50\% \text{Li}_2\text{WO}_4 + 50\% \text{K}_2\text{SO}_4) - (50\% \text{Li}_2\text{SO}_4 + 50\% \text{K}_2\text{WO}_4) - \text{K}_2\text{Cl}_2$, as shown in Fig. 7. This section is obtained by a diagonal cut through the prism side which depicts the $\text{Li}, \text{K} // \text{SO}_4, \text{WO}_4$ reciprocal ternary system. In the quaternary reciprocal system $\text{Li}, \text{K} // \text{Cl}, \text{SO}_4, \text{WO}_4$, this section represents a simple ternary eutectic system with an invariant point at approximately 13% K_2Cl_2 , 57% D_1 and 30% D_2 and represents a stable diagonal section of the prism depicting the composition of the given system.

Inner Triangular Section

Fig. 7



This section, inside the prism, cuts through only three of the total of four volumes of crystallization, namely, K_2Cl_2 , D_1 and D_2 .

In the ternary reciprocal system $\text{Li}, \text{K} // \text{SO}_4, \text{WO}_4$, represented as a prism, we have a "belt-a-diagonal" system, the general character of which principally determines the character of our quaternary reciprocal system, and the simple eutectic characteristics of the inner triangular section (Fig. 7). Fig. 8 represents the scheme of unfolded sides of the prism of composition system $\text{Li}, \text{K} // \text{Cl}, \text{SO}_4, \text{WO}_4$. With the increase of the number of crystallization volumes by the presence of the two double salts, the number of stable temperatures is also increased.

Scheme of unfolded sides of the prism of composition

Fig. 8

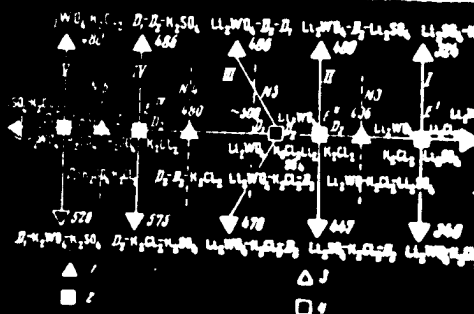


TABLE 3

Tetra- hedron	Point	Character	Composition, Volume %	Equilibrium Solid Phases
I	I	Quaternary Eutectic	64 36 78 18 4	Li_2WO_4 , Li_2SO_4 , K_2SO_4 , K_2Cl_2
II	II	Quaternary Eutectic	80 20 20 64 16	Li_2WO_4 , D_2 , Li_2SO_4 , K_2SO_4
III	P	Transition	73 27 18 43 39	Li_2WO_4 , D_2 , D_1 , K_2SO_4
IV	IV	Quaternary Eutectic	42 58 10 32 58	D_1 , D_2 , K_2SO_4 , K_2Cl_2
V	V	Quaternary Eutectic	27 73 16 12 62	D_1 , K_2Cl_2 , K_2WO_4 , K_2SO_4

Scheme of Crystalline
"tree" for the system
 $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$

Fig. 9



1. Ternary eutectics. 2. Quaternary eutectics. 3. Ternary transition points.
4. Quaternary transition points.

This is also verified by the study of the $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$ system, outlined by the authors as an example. By means of a number of inner sections, shown earlier in Fig. 2, it is shown that the above system can be divided by 4 such inner sections into five tetrahedrons each of which has a quaternary eutectic point, while the fifth tetrahedron has a quaternary transition point. Their compositions are listed in Table 3.

The visual confirmation of these data are shown schematically in Fig. 9.

CONCLUSION

1. The study of complex formation of the quaternary reciprocal system $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$ is reported in this article.
2. Formation of two double salts $\text{Li}_2\text{WO}_4 \cdot \text{K}_2\text{WO}_4$ and $\text{Li}_2\text{SO}_4 \cdot \text{K}_2\text{SO}_4$ in the ternary reciprocal system $\text{Li, K} // \text{SO}_4, \text{WO}_4$, which forms a vertical side of the prism for the quaternary system $\text{Li, K} // \text{Cl, SO}_4, \text{WO}_4$, is shown.
3. The three book section:
 - I. (50% Li_2WO_4 + 50% Li_2SO_4) - (50% K_2WO_4 + 50% K_2SO_4) - Li_2Cl_2 - K_2Cl_2
 - II. (80% Li_2WO_4 + 20% Li_2SO_4) - (80% K_2WO_4 + 20% K_2SO_4) - Li_2Cl_2 - K_2Cl_2
 - III. (30% Li_2WO_4 + 70% Li_2SO_4) - (30% K_2WO_4 + 70% K_2SO_4) - Li_2Cl_2 - K_2Cl_2

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and one inner section ($50\% \text{Li}_2\text{WO}_4 + 50\% \text{K}_2\text{WO}_4$) - ($50\% \text{Li}_2\text{SO}_4 + 50\% \text{K}_2\text{SO}_4$) - K_2Cl_2 show the stability of Li_2WO_4 , K_2WO_4 and Li_2SO_4 , K_2SO_4 double salts. The inner boundaries of their crystallization volumes have been described.

4. The inner structure of the prism $\text{Li, K, // Cl, SO}_4, \text{WO}_4$ has been studied and found to have 8 volumes of crystallization - two of the above mentioned double salts and six of the single components.

5. The overall character of the ternary reciprocal system $\text{Li, K // Cl, SO}_4, \text{WO}_4$ is discussed in detail.

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